## Calculus with Polar Coordinates: Examples

1. Find the area enclosed by $r=3+2 \sin \theta$
2. Find the area enclosed by the spiral $r=e^{\theta}$, where $\theta \in[0, \pi]$
3. Find the area of the inner loop of the curve $r=1-2 \sin \theta$
4. Find the area of the region that lies inside the curve $r=3 \cos \theta$ and outside the curve $r=1+\cos \theta$.
5. Find the slope of the polar curve $r=e^{\theta / 2}$ at the point $(1,0)$
6. Find the equation of the tangent line to the curve $r=\sin (2 \theta)$ when $\theta=\pi / 2$
7. Find all points where $r=3+\sin \theta$ has a horizontal tangent.
8. Find all points where $r=\sin ^{3} \theta$ has a vertical tangent.
9. Set up the integral that gives the length of the curve $r=3+\sin \theta$
10. Find the length of the curve $r=2^{\theta}, 0 \leq \theta \leq \pi / 2$
