Parametric Equations: Examples

1. A parametric curve is given by $x = 3 \sin t$, $y = 2 \cos t$, where $-\pi \le t \le \pi$. Sketch the curve by using the parametric equations to plot points. Indicate with an arrow the direction in which the curve is traced as t increases.

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2. Sketch the curve given by

$$\begin{aligned} x &= t+1 \\ y &= t^2, \qquad -2 \leq t \leq 1 \end{aligned}$$

- 3. Consider the parametric curve given by $x = e^t + 1$, $y = e^{2t}$. Eliminate the parameter to find a Cartesian equation of the curve.
- 4. Find a Cartesion equation for the curve given by the parametric equations $\begin{cases} x = 2t 1\\ y = \ln(t) \end{cases}$
- 5. Find a Cartesion equation for the curve given by the parametric equations $\begin{cases} x = \sin t \\ y = \cos^2 t \end{cases}$

6. Find a Cartesion equation for the curve given by the parametric equations $\begin{cases} x = 2 \sec t \\ y = 3 \tan t \end{cases}$

- 7. Find a parametrization for the hyperbola $x^2 \frac{y^2}{4} = 1$
- 8. Find a parametrization for the curve $y^3 + x^2 = 64$
- 9. Find 2 parametrizations for the curve $y = x^2 + 4x + 4$